

# An Embedding Approach to Anomaly Detection

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# Motivation

## ➤ Anomaly detection

- Identification of patterns in data that do not conform to expected behaviors [Chandola et al. 2009]
- Useful in a wide variety of applications



## ➤ In networks, anomaly detection has broader meanings

- **Application-specific significance**
- **Possibility to improve the performance of network-centric mining tasks such as community detection and classification**

# Motivation

- Structural hole theory [Burt 1992, 2004]
  - Theory of social capital
  - A structural hole is a gap between two nodes who have complementary sources to information



Prof. Ronald S. Burt



How to detect social brokers?

A formal quantitative definition is needed in the first place!

structural  
hole



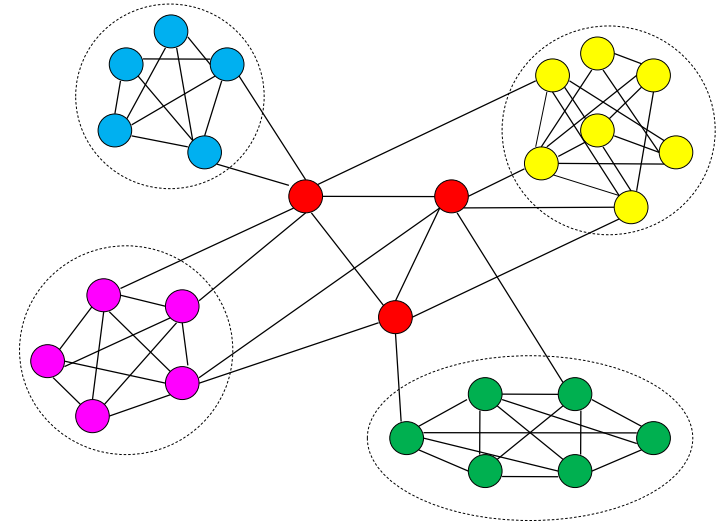
B

- **Node A (social broker)** is more likely to get novel information than B, even though they have the same number of links.

# Motivation

## ➤ Structural inconsistencies

- Nodes that connect to a number of diverse influential communities
- Detect social brokers quantitatively



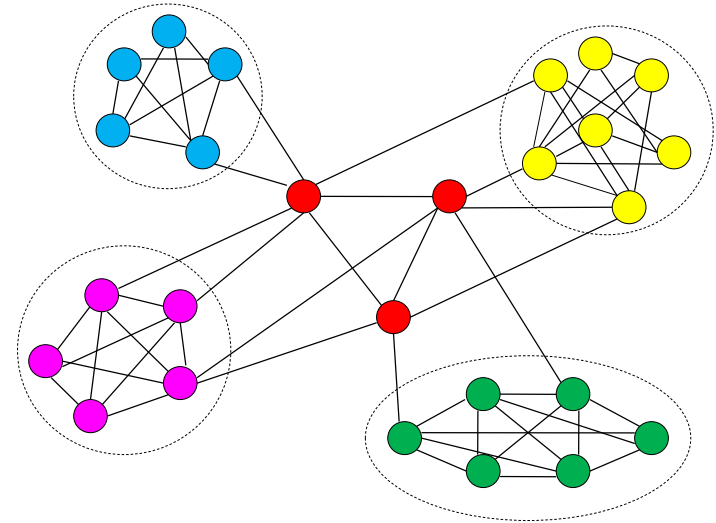
## ➤ Anomalousness from homophily [McPherson et al. 2001]

- Linked nodes have similar properties
- Fundamental to a wide variety of algorithms in network science
  - ✓ *E.g.*, community detection, collective classification, link prediction, influence analysis
- **Violated by structural inconsistencies**

# Motivation

## ➤ Structural inconsistencies

- Nodes that connect to a number of diverse influential communities
- Detect social brokers quantitatively



## ➤ The presence of structural inconsistencies may:

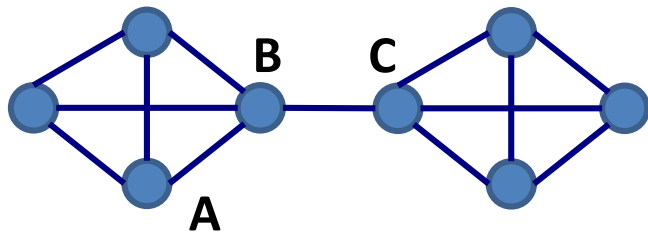
- have a substantial impact on network structure
  - ✓ *E.g.*, all nodes tend to form one large cluster
- prevent effective applications of network mining algorithms
  - ✓ *E.g.*, hard for community detection algorithms to achieve meaningful clusters

# Outline

- Anomaly detection model
  - Graph embedding
  - A quantitative measure of anomaly
- Algorithm optimization techniques
- Evaluation

# Why graph embedding?

- Structural inconsistencies
  - connect to a number of diverse influential communities
- Evaluate the diversity or similarity of nodes. How?



- To node B, node A is more similar than C, even though they have the same (global) distance from B.

- Graph embedding
  - Associate each node with a multidimensional vector
  - Preserve local linkage structure (instead of global structure)
  - Each dimension corresponds to a community in the network

# Why graph embedding?

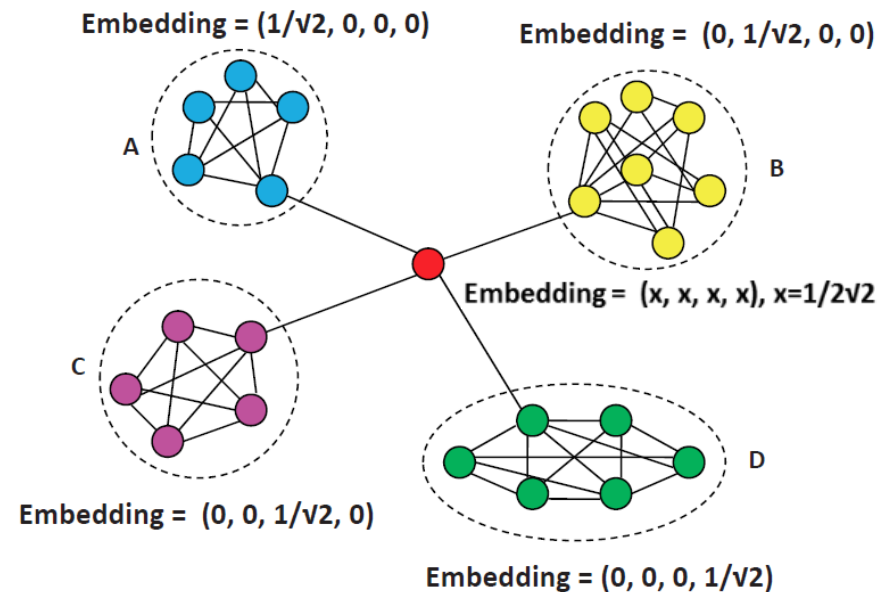
- Structural inconsistencies
  - connect to a number of diverse influential communities
- An alternative option: doing community detection followed by anomaly detection
  - Do not distinguish anomalies from normal nodes
  - The presence of anomalies has certain impacts on the results of community detection
  - Community detection is a heavy task.
  - Fail to detect structural inconsistencies!



# Graph embedding

- Given an undirected graph  $G=(V, E)$ , associate each node  $i$  with a  $d$ -dimensional vector  $X_i$

- $V = \{1, 2, \dots, n\}$
- $d$  : number of communities
- $X_i$  : correlation between node  $i$  and the  $d$  communities



A reasonable selection of  $d$  suffices for anomaly detection.  
Not necessary to use the number of real-life communities.

# Graph embedding

- Given an undirected graph  $G=(V, E)$ , associate each node  $i$  with a  $d$ -dimensional vector  $X_i$

- **Goal: preserve local linkage structure**

- Connected nodes should have similar values of  $X_i$
- Disconnected nodes should have diverse values of  $X_i$

- **Computation: minimizing objective function  $O$**

$$O = \sum_{(i,j) \in E} \|X_i - X_j\|^2 + \alpha \cdot \sum_{(i,j) \notin E} (1 - \|X_i - X_j\|)^2, \alpha = \frac{m}{\binom{n}{2} - m}$$

- $n$ : number of nodes in  $G$ ,  $m$ : number of edges in  $G$
- $\alpha$  : balancing factor that regulates the importance of the two components in  $O$
- The embedding ensures that  $0 \leq \|X_i - X_j\|^2 \leq 1$

# A quantitative measure

- Inspired by structural inconsistencies and structural holes (social brokers)
  - Connect to a number of diverse influential communities
  - Bridge across complementary sources

- *NB(i)*: how node *i* connects to communities

$$NB(i) = (y_i^1, \dots, y_i^d) = \sum_{(i,j) \in E} (1 - \|X_i - X_j\|) \cdot X_j$$

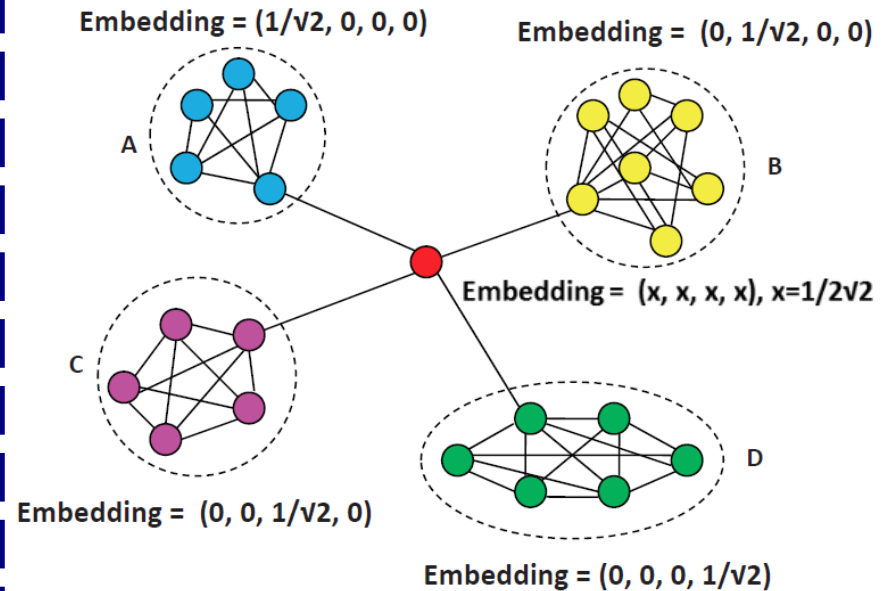
- *AScore(i)*: the anomalousness of node *i*

$$AScore(i) = \sum_{k=1}^d \frac{y_i^k}{y_i^*}, y_i^* = \max \{y_i^1, \dots, y_i^d\}$$

- Detect anomalies by *AScore(i) > thre*

# Example

- Optimality of embedding, *i.e.*, minimum value of  $O$ 
  - **Small values** within groups because of missing edges
  - **No values** across groups
  - **Certain values** for the red node (no better embedding)
  
- Anomalousness of nodes
  - **$AScore(red) = 4$**  (equal values in dimensions of  $NB(red)$ )
  - **$AScore(i) \approx 1$**  for others ( $NB(i)$  only has a dominating dimension)



$$O = \sum_{(i,j) \in E} \|X_i - X_j\|^2 + \alpha \cdot \sum_{(i,j) \notin E} (1 - \|X_i - X_j\|)^2$$

$$AScore(i) = \sum_{k=1}^d \frac{y_i^k}{y_i^*}, y_i^* = \max \{y_i^1, \dots, y_i^d\}$$

**The red node is detected as an anomaly!**

# Outline

- Anomaly detection model
- Algorithm optimization techniques
  - Sampling
  - Graph partitioning based initialization
  - Dimension reduction
- Evaluation

# Issues in the model

- Objective function  $O$  is a sum over  $O(n^2)$  terms
  - Forbidden in large social networks
- Optimizing  $O$  uses a gradient descent method
  - Critically dependent on a good initialization
- Dimensionality of embedding (*i.e.*,  $d$ ) could be large
  - *E.g.*, 8,353 for YouTube and 6,288,363 for Orkut [Yang & Leskovec 2012]

# Sampling

- Objective function  $O$  is a sum over  $O(n^2)$  terms

$$O = \sum_{(i,j) \in E} \|X_i - X_j\|^2 + \alpha \cdot \sum_{(i,j) \notin E} (1 - \|X_i - X_j\|)^2, \alpha = \frac{m}{\binom{n}{2} - m}$$

- Observation: balancing factor  $\alpha$  is close to 0
  - Very inefficient
  - Possible to approximately represent  $O$  by sampling

- Sampled objective function  $O$

$$O \approx \sum_{(i,j) \in E} \|X_i - X_j\|^2 + \sum_{(i,j) \in E_s} (1 - \|X_i - X_j\|)^2, E_s \subset \{(i,j) \mid (i,j) \notin E\}$$

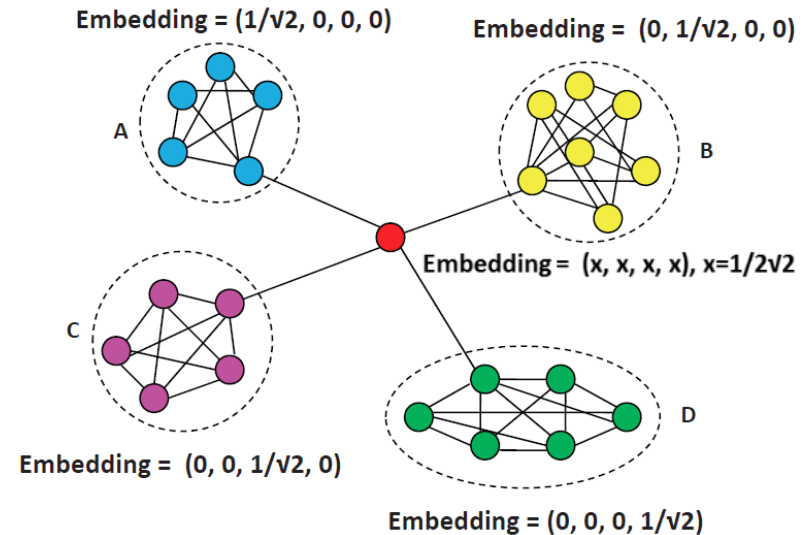
- $|E_s| = |E| = m$

# Graph partitioning based initialization

- Optimizing  $O$  uses a gradient descent method
  - Critically dependent on a good initialization

- A good initialization means small value of  $O$

- Densely connected nodes have similar values of  $X_i$
- Nodes across groups have diverse values of  $X_i$



- Incorporating graph partitioning (METIS) for initialization

- $P_i$ : partition number of node  $i$

$$X_i = (x_i^1, \dots, x_i^d), x_i^j = \begin{cases} 1/\sqrt{2} & j = P_i \\ 0 & j \neq P_i \end{cases}$$

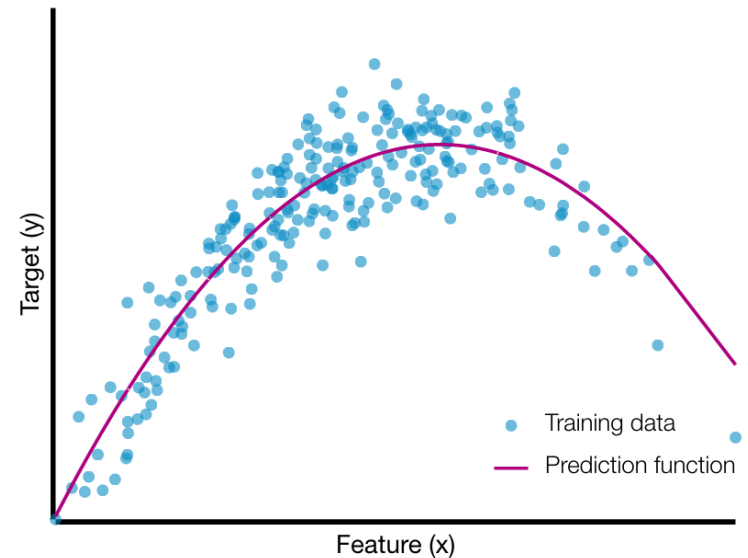


# Dimension reduction

➤ Dimensionality of embedding (*i.e.*,  $d$ ) can be large

➤ The complete  $d$ -dimensions are **unnecessary**

- Nodes typically connect to a limited number of communities
- A limited number of communities suffice to ascertain anomalies



**(Gordon) Hughes Effect**

➤ Data approximation ( **$k+\beta$  reduction**)

- only maintain  $(k+\beta)$ -dimensions for embedding of each node
- $k$  : the maximum number of communities to connect
- $\beta$  : tolerate mistakes when determining the  $k$  communities
- $k \ll d$  &  $\beta \ll d$ , *e.g.*, 10 & 2 for a network with  $n = 10^6$

# Impacts of optimization techniques

	Space	Efficiency	Effectiveness
<b>Sampling</b>	/	Prev.: $O(n^2 \cdot d)$	Remain effective (from experiments)
		After: $O(m \cdot d)$	
<b>Graph partitioning</b>	/	Prev.: 0	Provide a good initialization
		After: $O(n+m+d \cdot \log(d))$	
<b><math>k+\beta</math> reduction</b>	Prev.: $O(n \cdot d)$	Prev.: $O(t \cdot m \cdot d)$ $t$ : # of iterations	Slightly improve effectiveness
	After: $O(n \cdot (k+\beta))$	After: $O(t \cdot m \cdot (k+\beta))$	

# Outline

- Anomaly detection model
- Algorithm optimizations
- Evaluation

# Experimental settings

## ➤ Datasets

Dataset	# of nodes	# of edges	Descriptions
Amazon	334,863	925,872	Product co-purchasing
DBLP	1,150,852	5,098,175	Co-authorship
Synthetic	$10^5 - 4 \times 10^6$	$m = n^{1.15}$	LFR-benchmark graph

- Anomaly injection on Synthetic data for ground-truth of anomalies

## ➤ Algorithms

- **Embed( $d$ )** : embedding of  $d$ -dimensions
  - **Embed( $k+\beta$ )** : embedding with  $k+\beta$  reduction
  - **Oddball** : based on violation of power-laws of egonet-based features
  - **MDS( $d$ )** : similar to Embed( $d$ ), except using multi-dimensional scaling for embedding (preserve global structure)
- Parameters:  $d = n/500$ ,  $k = avgDeg$ ,  $\beta = k/4$
- Implementation: C++, Core i5 3.10GHz, 16GB of memory

# Case study on DBLP

## ➤ Different people with the same name

### Wei Wang

- 84 people named Wei Wang [DBLP, May 10 2016]
- University of Waterloo (Canada), Fudan University (China), University of California, San Diego (USA), etc.

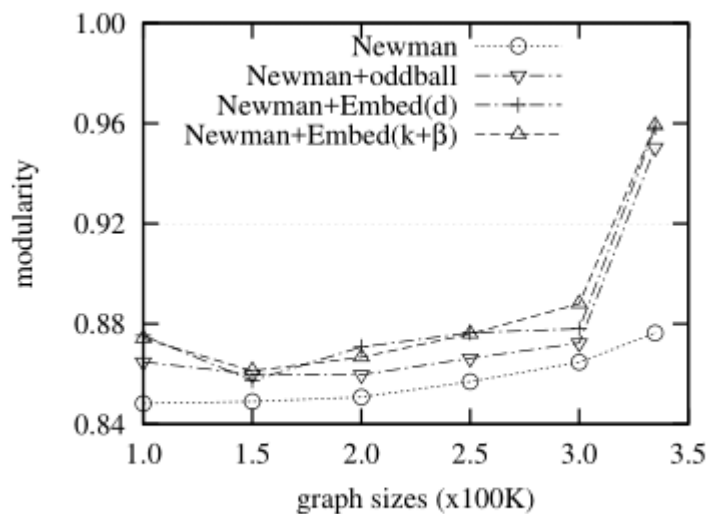
## ➤ People with many collaborators in diverse institutes

### Dr. Ajith Abraham

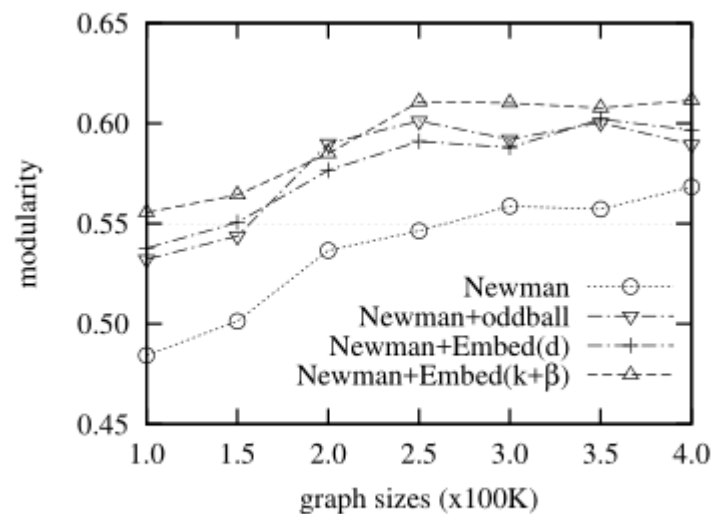
- Director of intelligence research labs which has members from more than 100 countries
- Work in a multi-disciplinary environment involving machine intelligence, cyber security, sensor networks and data mining
- Teach in 23 universities all over the world

# Quality study: modularity

- Modularity measures the strength of division of a network into communities
- Using modularity to evaluate the improvement of the effectiveness of community detection



(a) AMAZON dataset



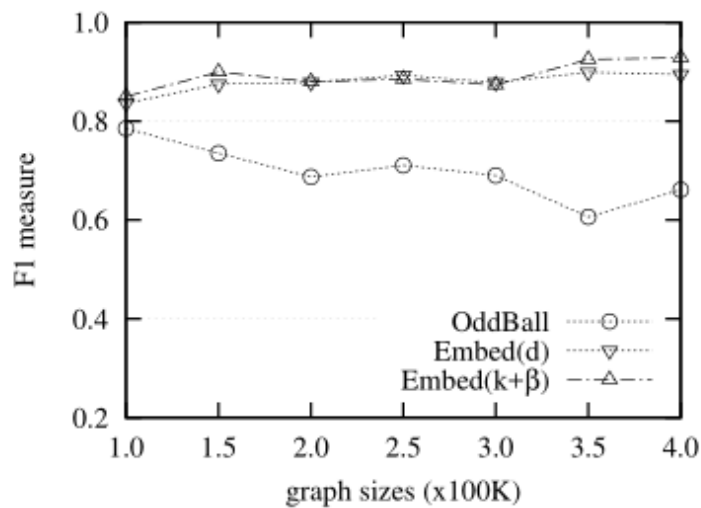
(b) DBLP dataset

	<b>oddball</b>	<b>Embed(<math>d</math>)</b>	<b>Embed(<math>k+\beta</math>)</b>
<b>Amazon</b>	2.1%	2.8%	<b>3.0%</b>
<b>DBLP</b>	4.2%	4.1%	<b>5.6%</b>

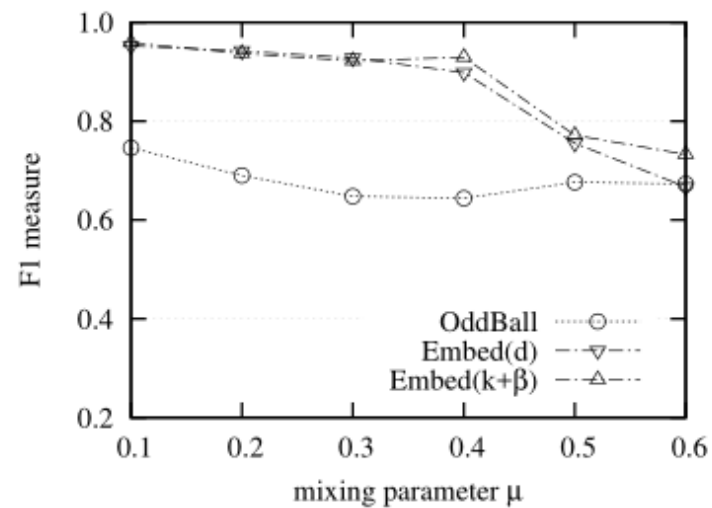
Table 1: Improvement of modularity

# Quality study: $F_1$ measure

- On Synthetic data with ground-truth of anomalies
- Mixing parameter  $\mu$ : fraction of inter-group edges (*i.e.*,  $\mu \uparrow$ , strength of community structure  $\downarrow$ )



(a)  $k + \beta$  reduction



(b) The mixing parameter  $\mu$

	<b>oddball</b>	<b>Embed(<math>d</math>)</b>	<b>Embed(<math>k+\beta</math>)</b>
<b>Varying graph sizes</b>	70%	88%	<b>89%</b>
<b>Varying <math>\mu</math></b>	68%	86%	<b>88%</b>

Table 2:  $F_1$  score of anomalies

# Impacts on quality: $d$ & embedding

- Synthetic data,  $n = 400K$ ,  $n/500 = 800$

	<b>MDS(<math>d</math>)</b>	<b>Embed(<math>d</math>)</b>
<b>d = 200</b>	11.3%	<b>89.4%</b>
<b>d = 400</b>	13.6%	<b>90.6%</b>
<b>d = 600</b>	12.7%	<b>89.8%</b>
<b>d = 800</b>	7.9%	<b>85.5%</b>
<b>d = 1000</b>	11.3%	<b>88.8%</b>
<b>Average</b>	11.3%	<b>88.8%</b>

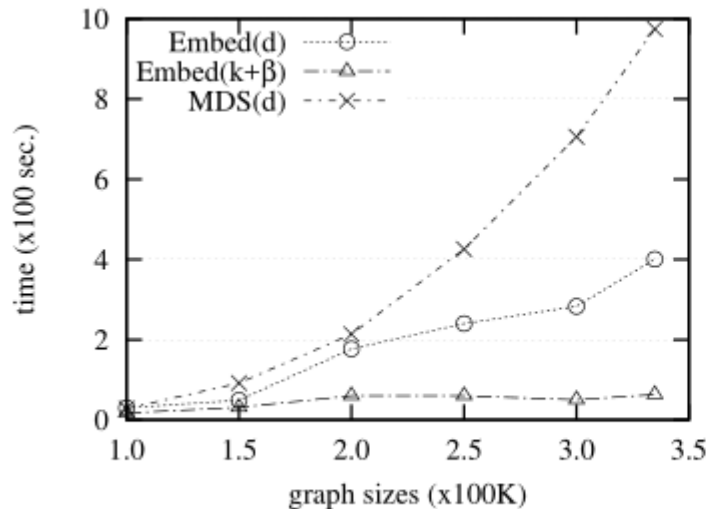
Table 3: MDS( $d$ ) vs. Embed( $d$ ) using  $F_1$  measure

- Multi-dimensional scaling fails to effectively detect anomalies
- Our approach works well as long as  $d$  falls into a reasonable range

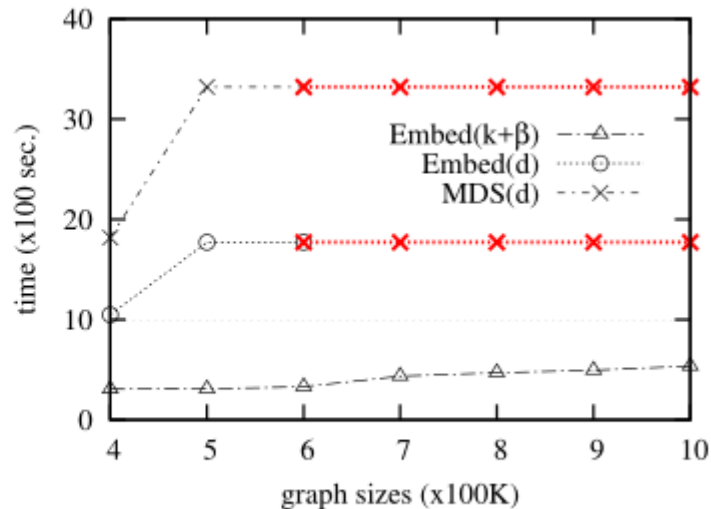


# Efficiency study

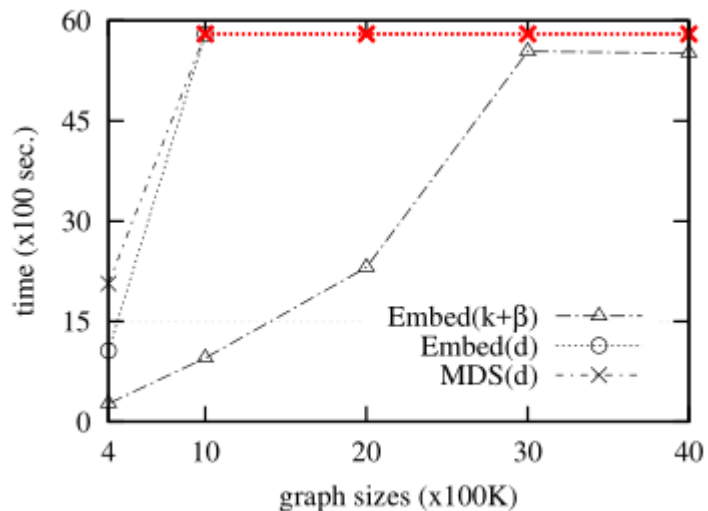
x : out of memory exception



(a) AMAZON dataset



(b) DBLP dataset



(c) SYNTHETIC dataset

	$E(k+\beta)/E(d)$	$E(k+\beta)/MDS(d)$
<b>Amazon</b>	35.3%	25.0%
<b>DBLP</b>	23.4%	13.1%
<b>Synthetic</b>	25.6%	13.2%

Table 4: running time comparison

# Summary

- **Structural inconsistencies**
  - Nodes that connect to a number of diverse influential communities
  - A formal quantitative definition of social brokers
- **An embedding approach**
  - Preserve local linkage structure of networks
  - A quantitative measure *Ascore* inspired by structural inconsistencies and structural holes
  - Three algorithm optimization techniques
- **Quality and efficiency results**
  - Modularity increases 2.9%, 4.9% and 6.9% on Amazon, DBLP and Synthetic data
  - F1 measure is 88% on Synthetic data
  - Running time increases reasonably *w.r.t* graph sizes

Thanks!

Q & A